

1st International High-Order CFD Workshop
Jan, 7-8, 2012, Nashville, TN

Summary of Test Case C1.5

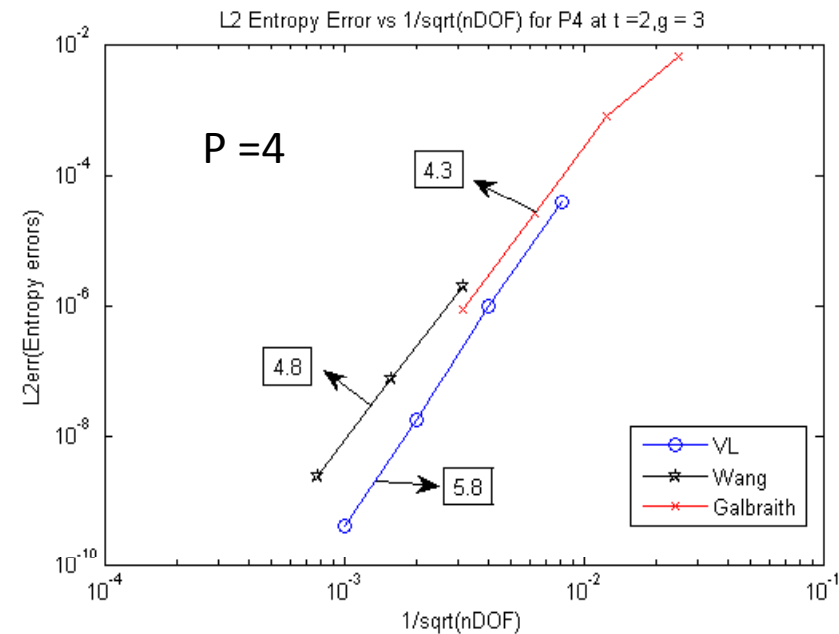
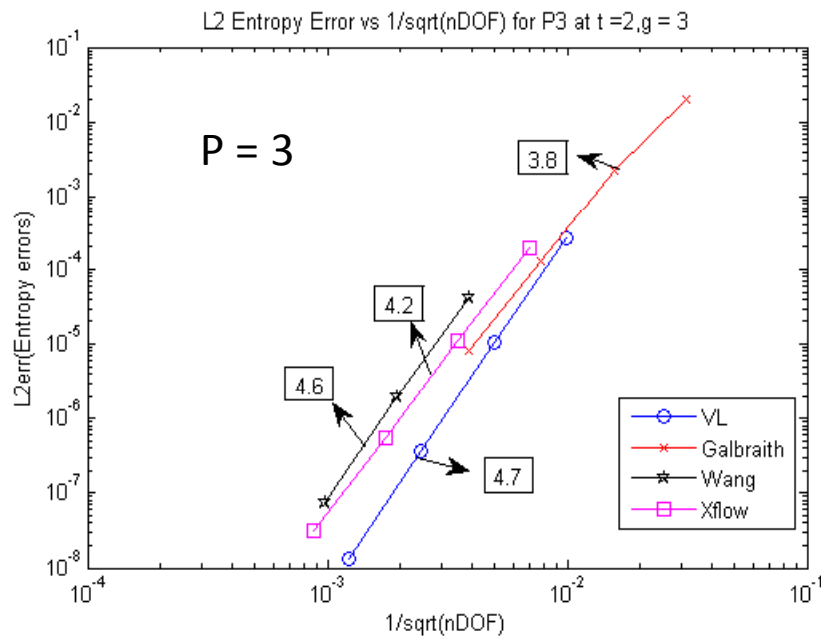
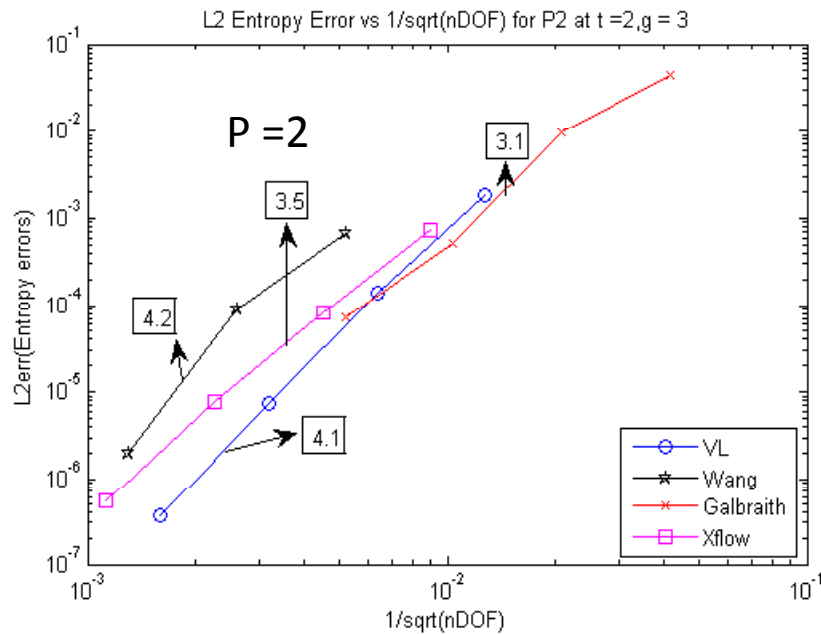
Radial expansion wave (2D/3D)

Contributing groups:

Fidkowski, Galbraith, Gassner,
Mavriplis, Van Leer, Z.J. Wang

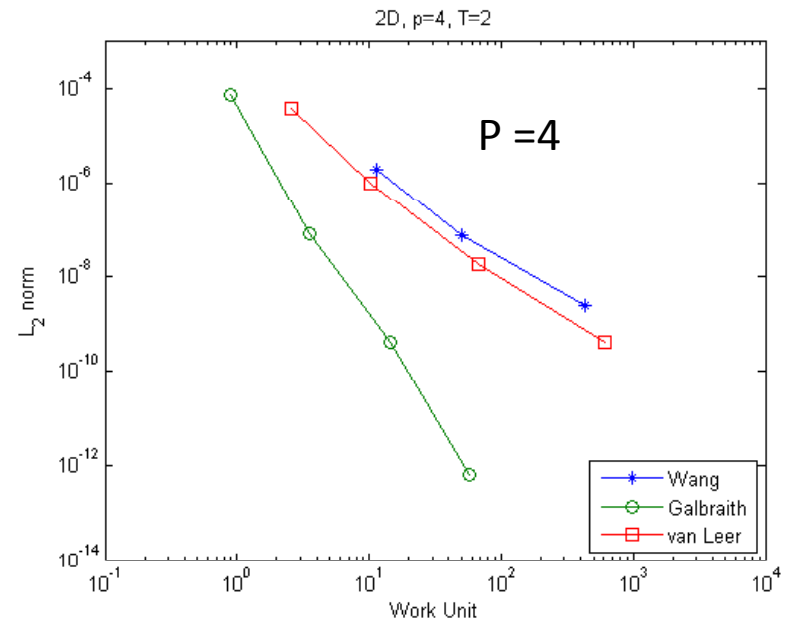
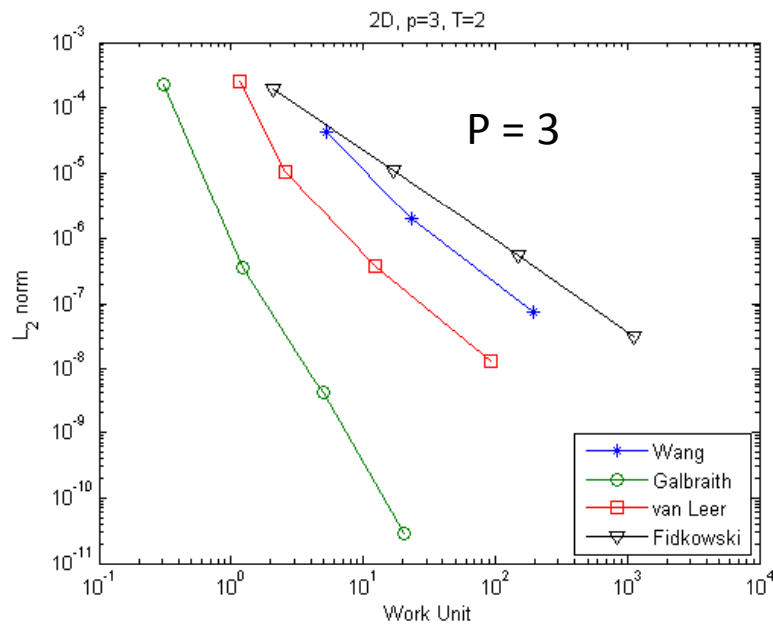
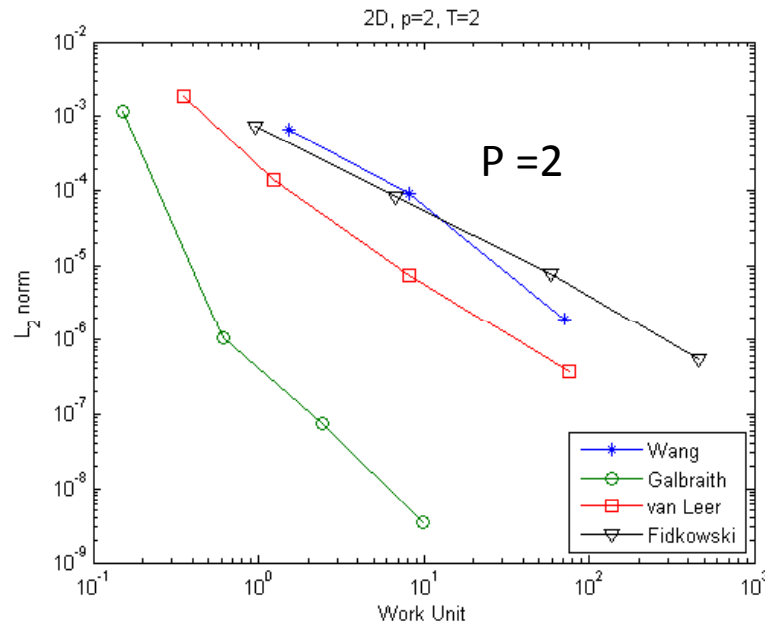
2D: Error vs. DOF

- Expected order: $2P+1$ on rectangles, $P+1$ on triangles.
- Order short of $2P + 1$ on rectangles.
- Cause: unexpected lack of solution smoothness at larger times.
- All results for $t=2, \gamma=3$, for greatest smoothness.
- Van Leer has lowest error.



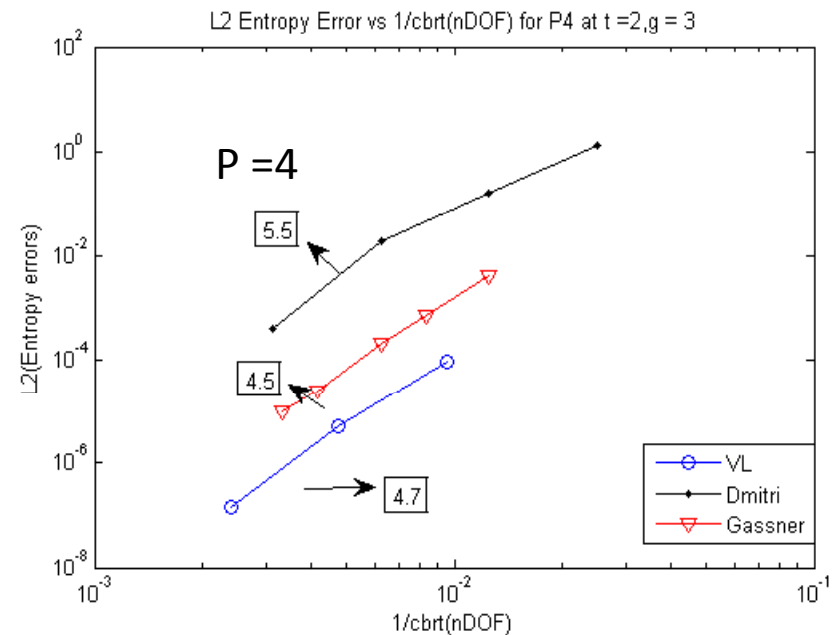
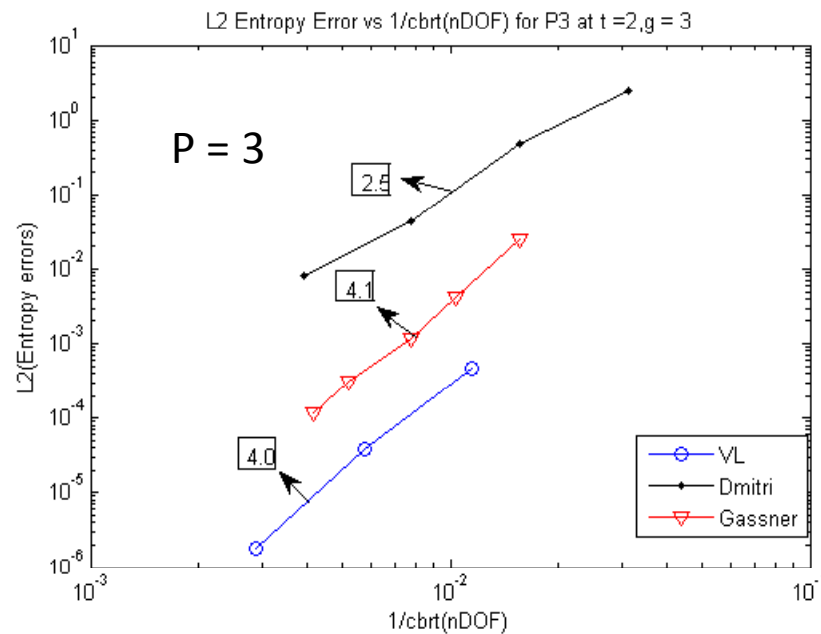
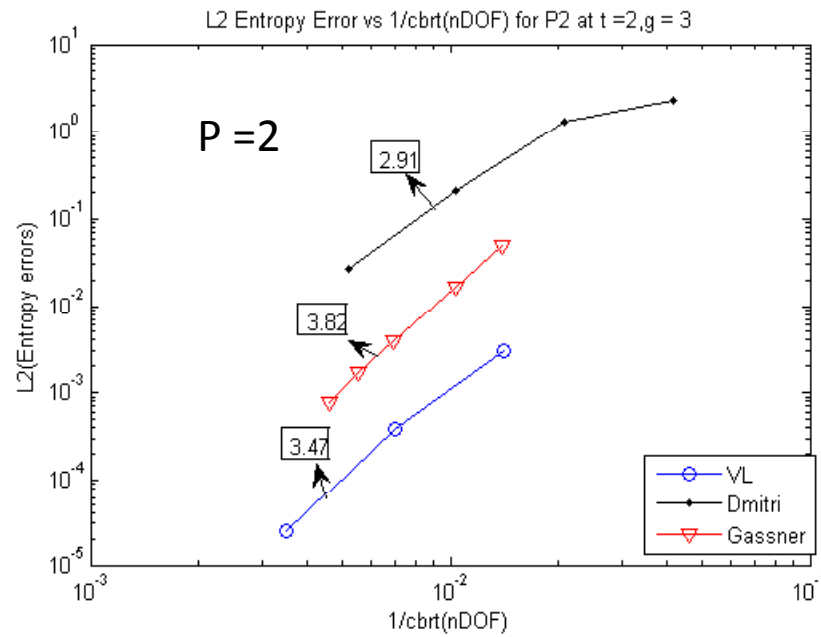
2D: Error vs. Work

- Galbraith most efficient owing to use of analytical integration rather than Gaussian quadrature.
- Van Leer second best.



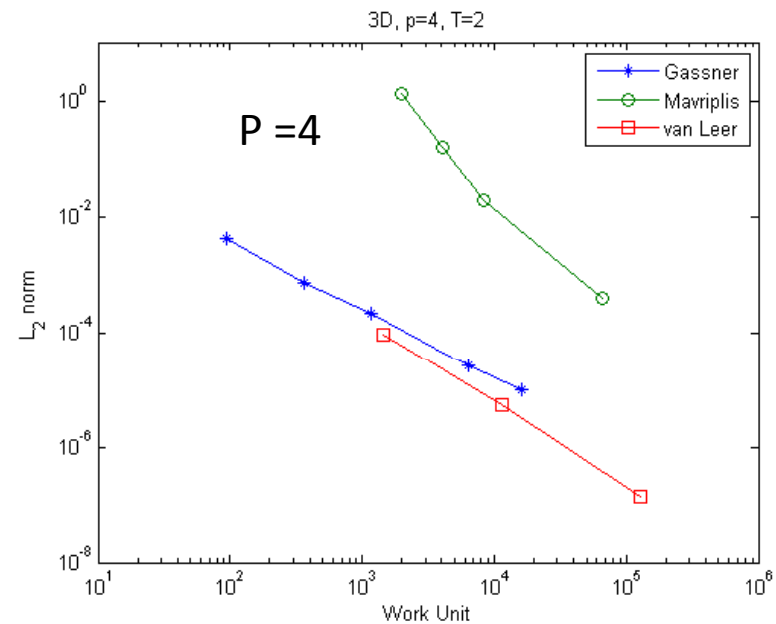
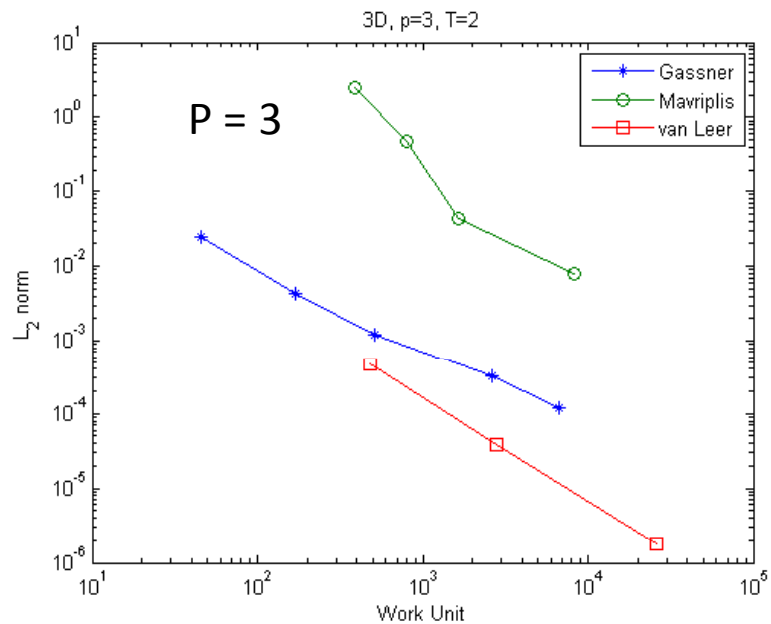
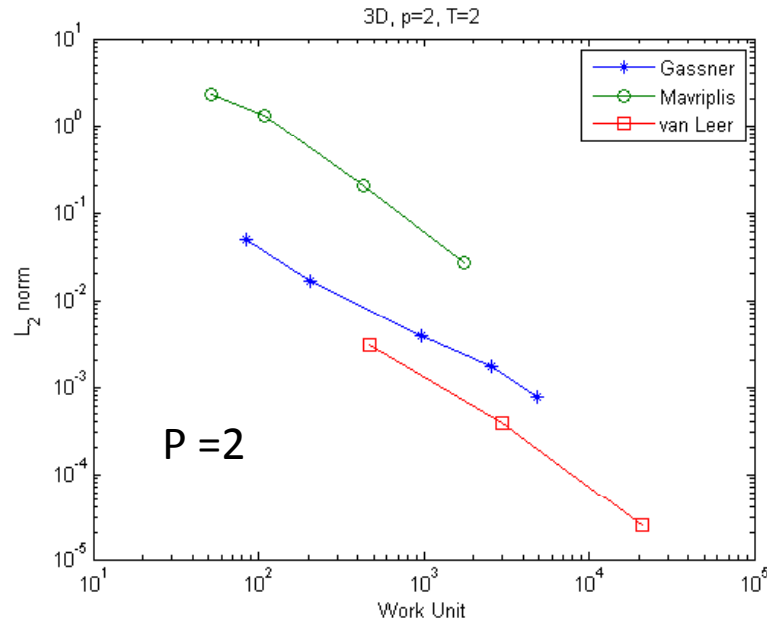
3D: Error vs. DOF

- Only regular hexahedral elements used.
- Results even further below expected order due to lack of solution smoothness.
- All results for $t=2, \gamma=3$.
- Van Leer has lowest error.



3D: Error vs. Work

- Only regular hexahedral elements used
- Van Leer most efficient.



Conclusions

- Before order of accuracy $2P+1$ can be reached with any DG method, the problem of the non-smoothness of the solution must be fixed, possibly by adding a manufactured source term.
- The consistently low errors of Van Leer et al. may be owing to high-order Gaussian quadrature used in anticipation of order of accuracy $2P+1$.